# A METHOD FOR COLLISION AVOIDANCE AND COLLISION MITIGATION

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#### TECHNICAL FIELD

The present invention relates to a method for avoiding collisions and collision mitigation involving vehicles and other objects. Specifically, the method is focused on predicting the probability density function for said vehicles and objects.

### BACKGROUND OF THE INVENTION

Several methods have been developed for collision avoidance utilizing sensors to obtain values such as distance, speed and direction of objects and vehicles.

US 4,623,966 discloses an apparatus for 15 collision avoidance for marine vessels. apparatus comprises sensing for providing means signals representative of the positions velocities of other vehicles relative to a first vehicle. These signals are used in a deterministic way to assess maneuvers of the first vehicle, which 20 avoid collision with the other vehicles. Collision danger is assessed through measures such as closest passing point, predicted point of collision and predicted areas of danger.

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Radar and laser are utilized in the invention disclosed in US 5,471,214 to detect objects within a specific range of the vehicle equipped with the collision avoidance system. The Kalman filter is used to estimate relative future positions of the

vehicles. A maximum danger region is defined and presence of an object in this region results in an alarm signal. Further, the invention is focused on the sensor set-up.

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Α similar system is disclosed in US 5,596,332. The Kalman filter is utilized predict future probable positions of aircrafts. the future probable position (a volume) at a specific time of an aircraft overlaps the future probable position at the same time for another aircraft, an alarm signal is generated. GPS is used to determine earth coordinates for the aircrafts.

15 US 6,026,347 discloses a method for use in vehicles to avoid collisions with obstacles. method applies to automated vehicles driving in the same direction in two or more lanes. Each vehicle includes a processor that is coupled to the vehicle's 20 braking, steering and engine management systems that can accept commands from other vehicles to brake, accelerate, or change lanes. The invention mainly concerns how coordination of maneuvers between several vehicles during avoidance maneuver should be 25 managed.

In US 6,085,151 a collision sensing system is disclosed where the probability of threat and the type of threat are computed, the result of which is used to perform an appropriate action, such as seat belt pre-tensioning, airbag readying and inflating,

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and braking. Thus, the main focus of the patent is preparing the vehicle for collision in order to enhance the safety. Individual targets are identified by clustering analysis and are tracked in a Cartesian coordinate system using a Kalman filter.

According to a paper by Jocoy al, "Adapting radar and tracking technology to an onboard automotive collision warning system", in: The AIAA/IEEE/SAE Digital Avionics systems Conference, 1998, Vol. 2, pp I24-1 - I24-8, the intersection collisions constitute approximately twenty-six percent of all accidents in the United States. A system is under development, which consists of a single radar assembly that will monitor vehicle traffic along the approaching lanes of traffic. A metric of gap time based on predicted time of arrival at the intersection is used to provide a warning to the driver. The measure used to detect threats is predicted as time to and out of the intersection.

A prediction system, which allows the evaluation of collision and unhooking risks in the automatic control of truck platoons on highways, is described in a paper by Attouche et al, "A prediction system based on vehicle sensor data in automated highway", In: 2000 IEEE Intelligent Transportation Systems, Conference Proceedings, 1-3 Oct. 2000, pp 494-499. The system applies to a concentration of trucks traveling in the same direction for long distances and comprises an inter-truck spacing signal

obtained by a triple measurement device: a laser range-finder, an embedded camera and a theoretical observer, based on system dynamic equations.

5 Α paper by Seki et al., "Collision avoidance system for vehicles applying predictive control theory", In: 1999 IEEE/IEEJ/JSAI International Conference on Intelligent Transportation Systems, 453-458, describes рp 10 similar system for avoiding collisions with vehicles or objects traveling in the same direction as the vehicle equipped with the collision avoidance system. What is discussed is mainly how to control the braking force, given some target stopping point which 15 is given by some safe deceleration rate plus surplus distance.

All of the above described prior collision avoidance systems and methods either are 20 dependant of external signal transmitters, example GPS satellite communication or communication between vehicles equipped with collision avoidance systems, or they result in giving alarm signals too frequently when implemented in an automobile. All of 25 the prior art systems or methods have difficulties handling situations like a vehicle meeting another vehicle traveling in the opposite direction on a two way road. If a collision avoidance system or method were to give an alarm signal every time the vehicle 30 equipped with such a system meets another vehicle, this would be a nuisance to the driver and could result in the driver shutting down the collision avoidance function and not using it at all.

## SUMMARY OF THE INVENTION

foregoing and other advantages provided by a method and apparatus for collision avoidance and collision mitigation. The present invention relates to a method for avoiding vehicle collisions and collision mitigation. The comprises the steps of predicting the probability density function (11, 12, 13, 14) for the position of 10 a vehicle at several future occasions and predicting the probability density function (21, 22, 23, 24) for at least one additional object at several future occasions. Further the method comprises the step of 15 forming the joint probability density function for the relative positions of the vehicle and object at several future occasions and integrating over the area in which the vehicle and object are in physical conflict.

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The present invention itself, together with attendant advantages, will be best understood by reference to the following detailed description, taken in conjunction with the accompanying figures.

#### 25 BRIEF DESCRIPTION OF THE DRAWINGS

In order that the invention may be well understood, there will now be described some embodiments thereof, given by way of example,

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reference being made to the accompanying drawings, in which:

Figure 1 shows a top view of two vehicles meeting on a straight road;

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Figure 2 shows a three-dimensional plot of the probability density functions for the vehicles in figure 1 at four different times;

- 10 Figures 3a and 3b show the probability density function in one direction for each of the two vehicles respectively at the four different times shown in figure 2;
- 15 Figures 4a-4d show for each of the four times in figure 2 the probability density function in one direction for each of the two vehicles; and

Figures 5a-5d show the joint probability 20 function in one direction for the two vehicles at the four different times shown in figure 2.

## BEST MODES FOR CARRYING OUT THE INVENTION

The method according to the invention will be explained with reference made to an example illustrated in the enclosed figures. The example is chosen in order to facilitate the reading and understanding of the method according to the present invention. Therefore, most of the diagrams in the

figures show the probability density functions in one direction.

Figure 1 illustrates a common situation with two vehicles meeting on a straight road. The 5 vehicle equipped with the collision avoidance system is denoted 10 and the other vehicle is denoted 20. example the probability density Throughout the function has been calculated for both the vehicles at 10 four future occasions (the same for both vehicles). The four future occasions are denoted 11, 12, 13 and 14, for the vehicle equipped with the collision avoidance system, with the same time interval between the future occasions. For the other vehicle the four future occasions are denoted 21, 22, 23 and 24. The 15 occasion 11 for the first said vehicle corresponds to occasion 21 for the other said vehicle and so forth for 12, 13 and 14. A time increment of 0.05 s in the example results in the velocities ~70 km/h and ~100 20 km/h (~45 mph and ~mph) for the vehicle equipped with the collision avoidance system and the other vehicle respectively.

probability In figure the functions have been calculated for the vehicles at 25 the four said future occasions and they are illustrated in this three-dimensional plot. The probability density functions 11 and 21 are the ones closest in time to the present location and thus the peaks are higher than for the functions 12, 13, 14, 30

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22, 23 and 24, i.e. the probabilities are high for the vehicles to be in this area. Contrary, the peaks of the probability density functions 14 and 24 are lower but the functions are on the other hand wider, the further away in the future The probability alternative positions. that vehicle ends up in a specific position is lower since the time difference between the present position and the future position is long and therefore larger changes can occur, for example changes in direction and velocity.

In figure 3a the probability density functions are shown in the direction of the vehicle equipped with the collision avoidance system at the four future occasions. Figure 3b illustrates the corresponding probability density functions for the other vehicle.

In figures 4a-4b the probability density functions have been divided up into four separate diagrams showing the probability density functions for both vehicles but where one diagram illustrates only one point in time. Thus, figure 4a shows the probability density functions 11 and 21, the closest in time to the present positions of the vehicles. Hence, the diagram in Figure 4b shows the probability density functions 12 and 22, the diagram in figure 4c shows the probability density functions 13 and 23 and the diagram in figure 4d shows the probability density functions 14 and 24. Preferably the time

intervals are chosen short. In figure probability density functions of the vehicles partly overlap each other. If, for example, interval had been twice as long (figures 4b and 4d) the probability density functions would pass each other, which then would result in a possible danger not being discovered. However, the calculations are repeated continuously with a frequency large enough to avoid such risks.

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Some prior art calculations are carried out i.e. the probability similar way, density functions are calculated for the vehicles. However, using prior art on the example here would result in alarm caused by the overlapping probability density functions 13 and 23 in figure 2 if the confidence interval is large. It is not desirable for a driver of a vehicle equipped with a collision avoidance system to have a warning signal every time said vehicle meets another vehicle in a situation similar to that in the example shown. The confidence interval might be chosen not to give warning signals in specific situations, but this will result in a relatively insensitive system that will fail to warn in some situations where a warning signal should be the result. According to the present invention a joint probability density function is therefore calculated for each of the future occasions. Figures 5a-5d show the joint probability density functions for one direction (traveling direction) example with four future occasions. The

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probability density function is integrated over the area in which the vehicle and object are in physical conflict. The output of the calculation indicate the probability of collision. However, figure 5c is the only figure showing any signal at all. Preferably a preset limit of when to alarm is chosen higher than the calculated probability in the example, since the situation is not one where an alarm signal desired. An alarm signal in a normal situation like this when the probability of collision is very low would be most annoying to the driver. However, the example shows only the probability density functions in only one direction. The probability of collision taking two dimensions into consideration, 15 example illustrated, is much lower. The probability density functions 13 and 23 seen along the traveling direction in figure 2 barely overlap. On the other hand, seen from the direction perpendicular to the traveling direction, as shown in figure 4c, the probability density functions overlap considerably.

Thus, the probability of collision for the vehicle and each of the surrounding objects should be calculated for a sufficient number of future occasions. Based on this, rules are set in the probability domain on when to take evasive action or The probability density function can for example be calculated by using the extended Kalman filter predict the vehicles and surrounding objects future positions as well as their associated covariance matrix. The following is

describing such a calculation. Calculating the probability density function using the Kalman filter is a relatively simple method. Much more sophisticated methods can be used instead but the simple method is used to facilitate the understanding of the concept according to the present invention. The algorithm uses the following discrete state space description for the vehicle and other objects:

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where:

 $X_{t} = \begin{pmatrix} x_{t} \\ y_{t} \\ v_{x,t} \\ v_{y,t} \\ m \end{pmatrix}$ 

 $x_t = x_t$  coordinate in a ground fixed 15 coordinate system

 $y_t = y_t$  coordinate in a ground fixed coordinate system

 $v_{x,t} = \text{velocity in the x direction}$ 

 $v_{y,t}$  =velocity in the y direction

20  $\omega_t$  = rate of direction change

$$X_{t+T} = \begin{pmatrix} 1 & 0 & \frac{\sin(\omega_{t}T)}{\omega_{t}} & \frac{-(1-\cos(\omega_{t}T))}{\omega_{t}} & \frac{v_{x}T\cos(\omega_{t}T)}{(\omega_{t}-\sin(\omega_{t}T))\omega_{t}^{2}} - \frac{v_{y}T\sin(\omega_{t}T)}{(\omega_{t}-(1-\cos(\omega_{t}T)))\omega_{t}^{2}} \\ 0 & 1 & \frac{1-\cos(\omega_{t}T)}{\omega_{t}} & \frac{\sin(\omega_{t}T)}{\omega_{t}} & \frac{v_{x}T\sin(\omega_{t}T)}{\omega_{t}-(1-\cos(\omega_{t}T)\omega_{t}^{2})} \frac{v_{y}T\cos(\omega_{t}T)}{\omega_{t}-\sin(\omega_{t}T)\omega_{t}^{2}} \\ 0 & 0 & \cos(\omega_{t}T) & -\sin(\omega_{t}T) & -v_{x}T\sin(\omega_{t}T)-v_{y}T\cos(\omega_{t}T) \\ 0 & 0 & \sin(\omega_{t}T) & \cos(\omega_{t}T) & v_{x}T\cos(\omega_{t}T)-v_{y}T\sin(\omega_{t}T) \end{pmatrix} X_{t}$$

$$= AX_{t}$$

The extended Kalman filter is used to predict the future positions of the vehicle and the objects. The Kalman filter prediction is iterated n times to obtain the vehicles position at the times T, 2T, ..., nT. For example, n is chosen so that nT is the same or slightly longer than the time it takes to come to a full stop given the speed, braking capabilities and the tire to road friction of the vehicle.

The main purpose of the decision-making algorithm is to get a measure of when to execute an avoidance maneuver or to make an alarm. The probability of the future positions of the vehicle and the object/objects being close to one another in the X and Y direction can be calculated as follows (in this example the coordinate system is fixed to the collision avoidance vehicle):

$$P_x(\Delta X | < a + b) = \int_{-a-b}^{a+b} f(\Delta X)$$

$$P_{y}(|\Delta Y| < c + d) = \int_{-c - d}^{c + d} f(\Delta Y)$$

where:

5  $\Delta X = {
m distance}$  between the vehicle and the object in the X direction

 $\Delta Y\!=\! \text{distance}$  between the vehicle and the object in the Y direction

a=half the width of the vehicle b=half the width of the object c=half the length of the vehicle d=half the length of the object

$$f(\Delta X) = \frac{1}{\sigma_x \sqrt{2\pi}} e^{\frac{-\Delta X^2}{2\sigma_v^2}} =$$

the probability density function of  $\Delta X$ 

$$f(\Delta Y) = \frac{1}{\sigma_y \sqrt{2\pi}} e^{\frac{-\Delta Y^2}{2\sigma_y^2}} =$$

the probability density function of  $\Delta Y$ 

 $\sigma_x$  and  $\sigma_y$  are given by the (1, 1) and (2, 2) elements of the covariance matrix of  $X_t$ ,  $P_t$ . The threshold for collision avoidance maneuver can be set to alarm when the probability  $P_x$  and  $P_y$  are greater than some values  $T_x$  and  $T_y$ .  $T_x$  and  $T_y$  are design

parameters who should be dependent on the velocity of the vehicle.

The foregoing is a disclosure of an example practicing the present invention. However, it is apparent that method incorporating modifications and variations will be obvious to one skilled in the art. Inasmuch as the foregoing disclosure is intended to enable one skilled in the art to practice the instant invention, it should not be construed to be limited thereby, but should be construed to include such modifications and variations as fall within its true spirit and scope.